

X-Ray Analysis

X-rays

- Originally discovered by Wilhelm Roentgen (1845-1923) in the nineteenth century, X-rays have become one of the most useful applications of spectroscopy in both science and medicine.



X-Ray Spectroscopy

- Emission
- Absorption
- Diffraction

X-ray spectroscopy is a common analytical technique with a broad range of applications, particularly in determining crystal structure and elemental analysis of solid samples.

Diffraction

wavelengths

0.1 $\Rightarrow$ 25Å

Diffraction

Powder Pattern

- qualitative analysis => ASTM database
- isostructural

X-ray for Analytical Purposes

X-ray for Analytical Purposes generated by:

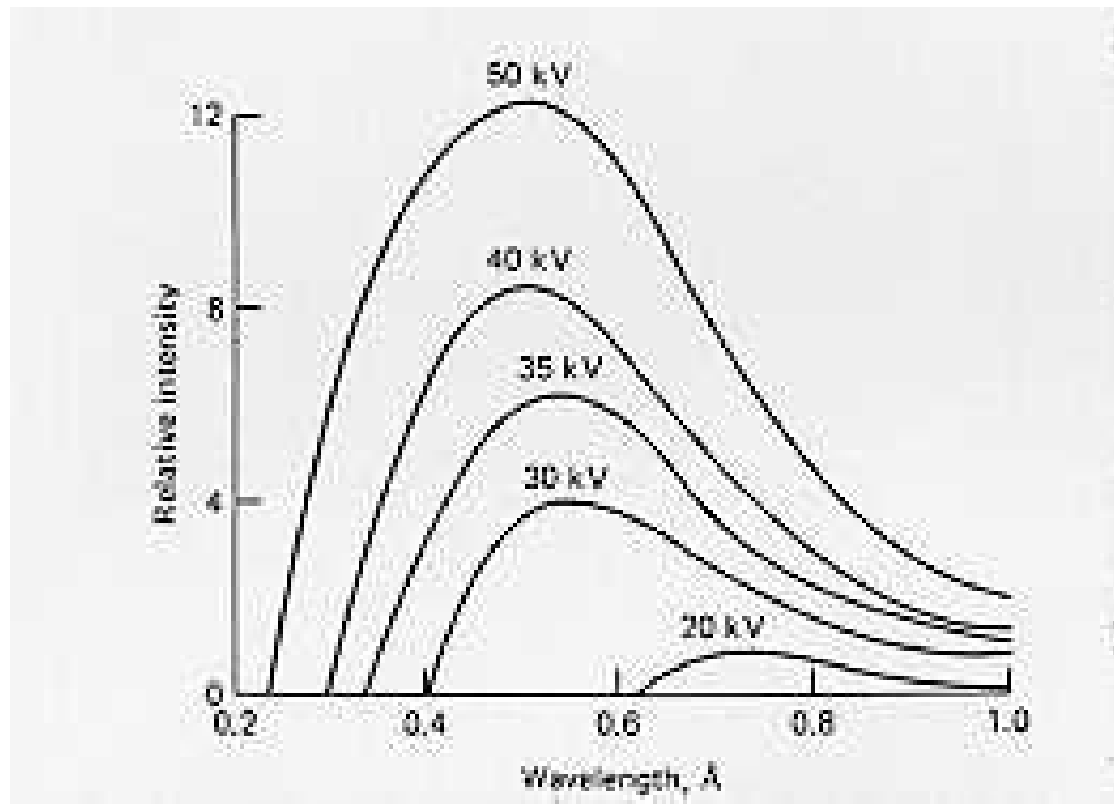
- 1. bombardment of metal target by a beam of high energy electrons**
- 2. exposure of a substance to a primary beam of X-rays in order to generate a secondary beam of fluorescent X-rays**
- 3. radioactive source whose decay process results in X-ray emission**

Production of X-rays

- The electromagnetic radiation resulting from inner orbital electron transitions or deceleration of high-energy electrons is referred to as X-rays.
- X-ray tubes
- Radio active materials
- Synchrotron source

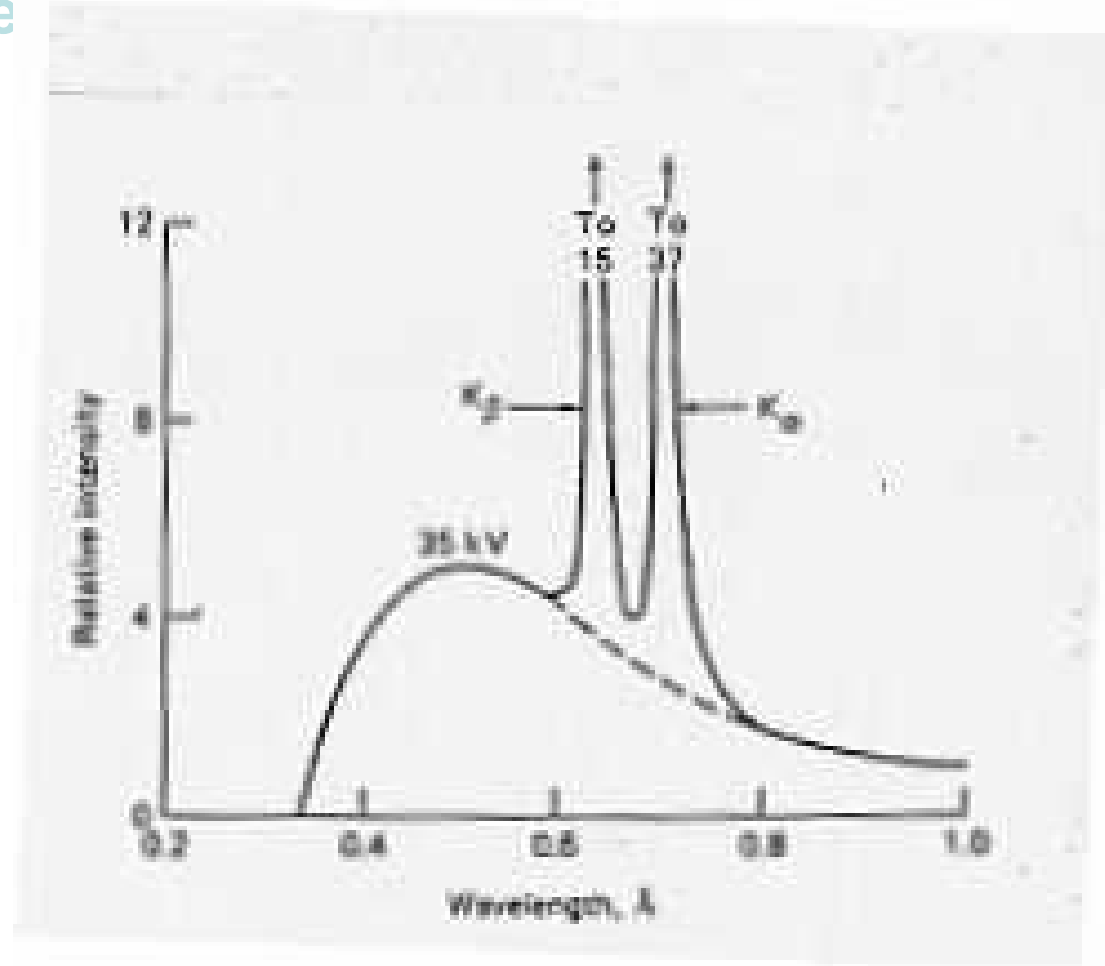
X-ray Tubes for Analytical Purposes

"Distribution of continuous radiation from an X-ray tube with a tungsten target. The numbers above the curves indicate the accelerating voltages."



X-ray for Analytical Purposes

"Line spectrum for a tube with a molybdenum target"



X-ray for Analytical Purposes

Short wavelength limit of continuum
function of accelerating voltage, not
metal

$$\lambda_o = 12,398/V$$

where $V \Rightarrow$ volts

X-ray for Analytical Purposes

2 series of lines for all metals $z > 23$

K & L series

1 series of lines for all metals $z < 23$

K series

line spectrum: min accelerating V to
produce increases with Z

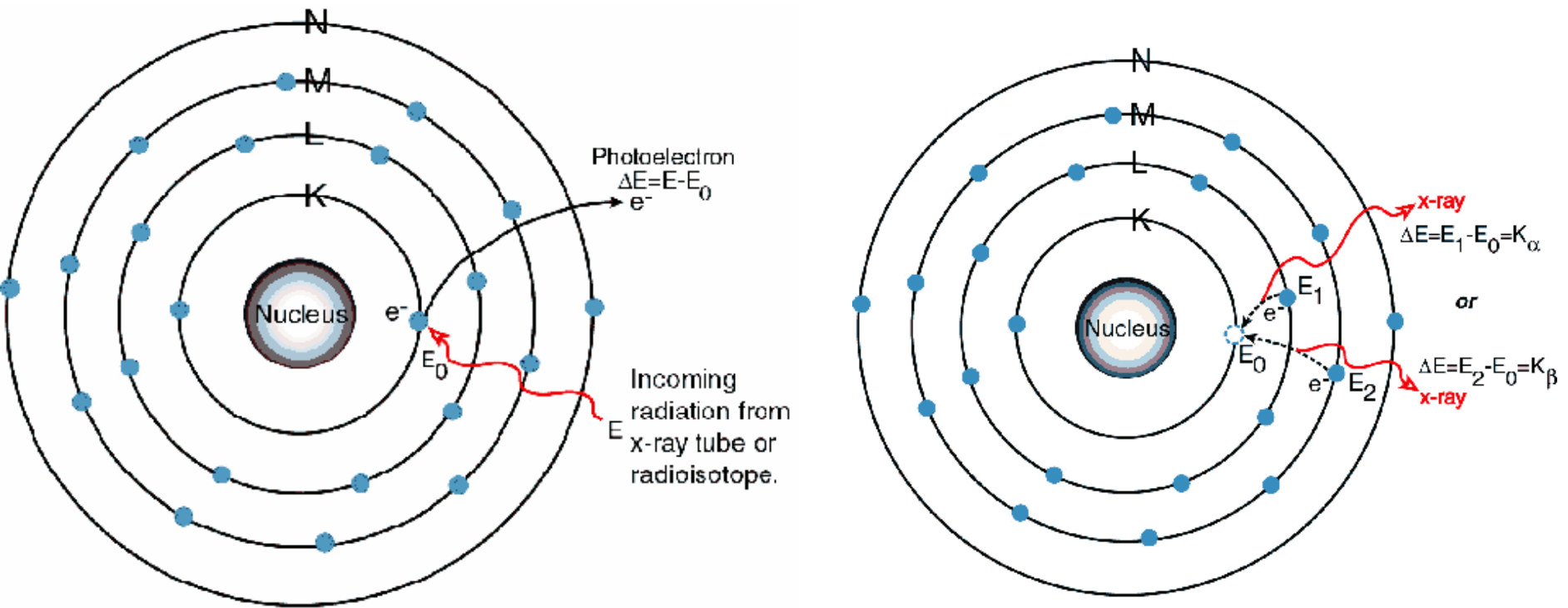
X-ray Fluorescence Spectroscopy-

- X-ray fluorescence is a spectroscopic method that is commonly used for solids in which secondary x-ray emission is generated by excitation of a sample with x-rays. The x-rays eject inner-shell electrons. Outer-shell electrons take their place and emit photons in the process. The wavelength of the photons depends on the energy difference between the outer-shell and inner-shell electron orbitals. The amount of x-ray fluorescence is very sample dependent and quantitative analysis requires calibration with standards that are similar to the sample matrix.

XRF Instrumentation

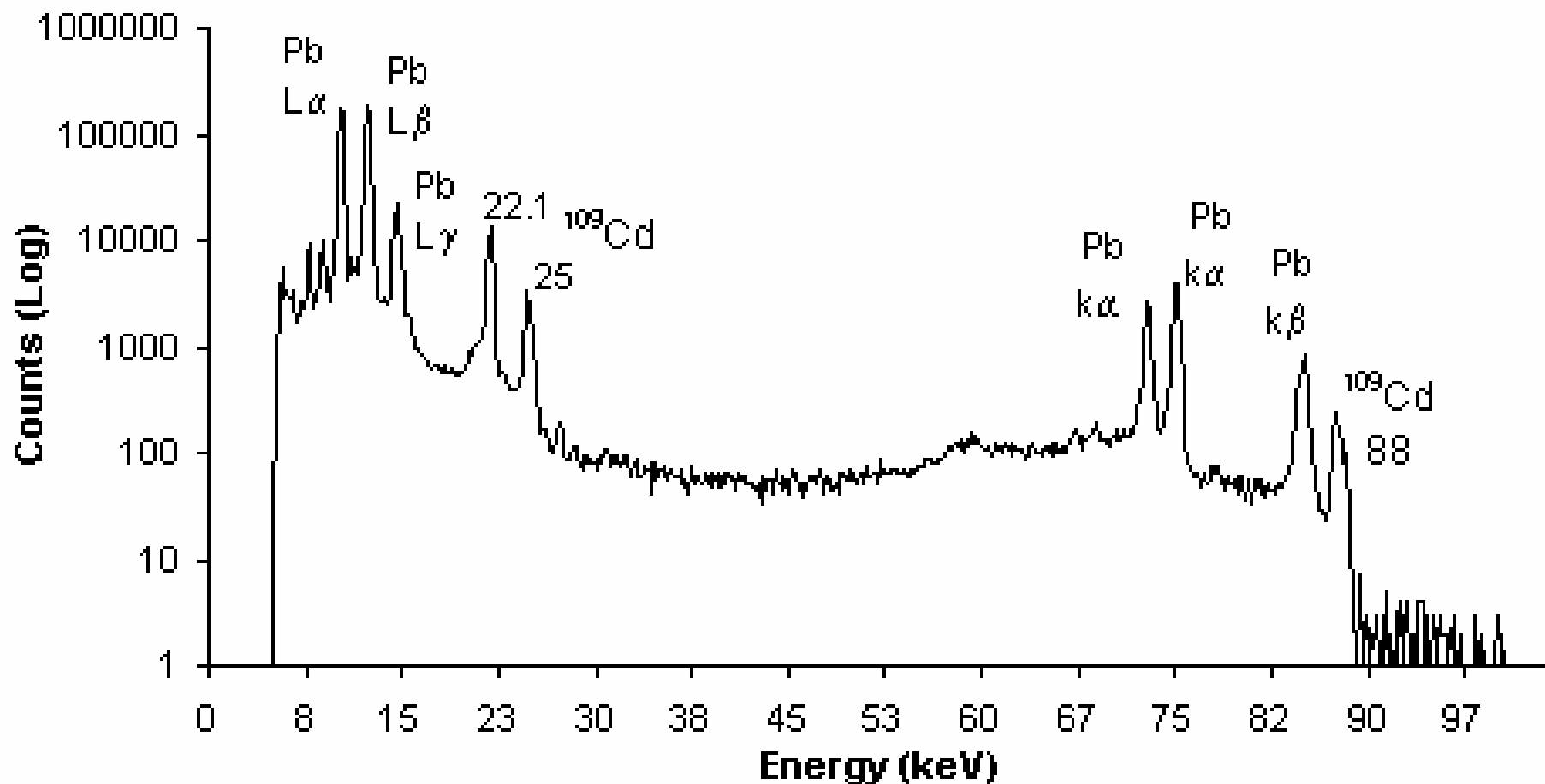
- Solid samples are usually powdered and pressed into a wafer or fused in a borate glass. The sample is then placed in the sample chamber of an XRF spectrometer, and irradiated with a primary X-ray beam. The X-ray fluorescence is recorded with either an X-ray detector after wavelength dispersion or with an energy-dispersive detector.

X-ray Fluorescence Spectroscopy- XRF

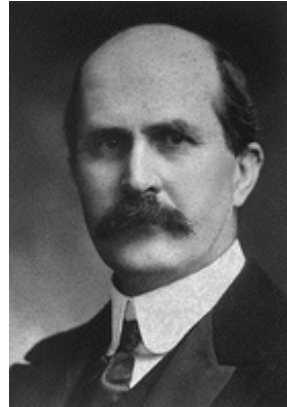


XRF Spectrum

X-Ray Fluorescence of Lead from ^{109}Cd



History of Diffraction

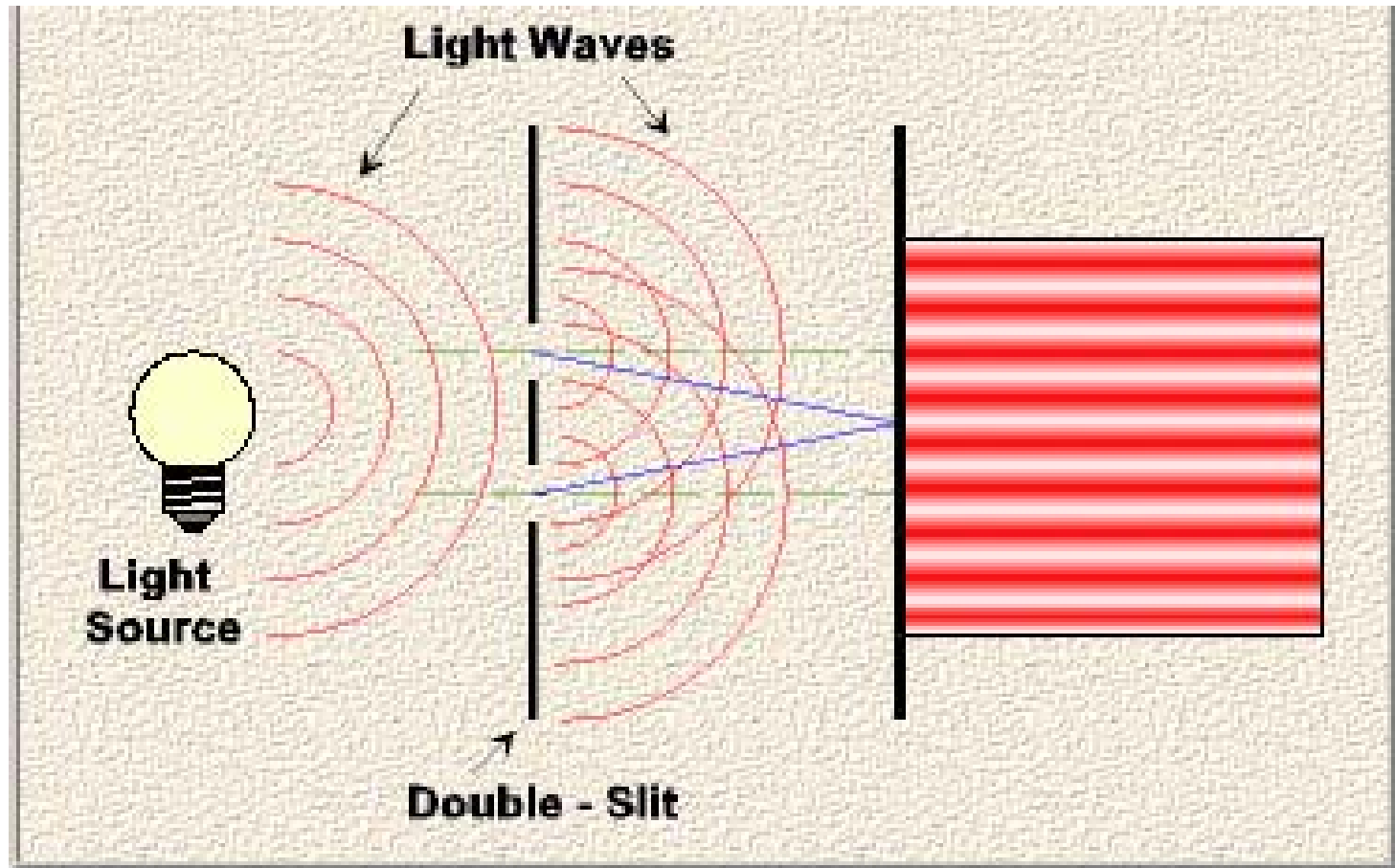


William Bragg and his son Lawrence

X-ray Diffraction

- William Bragg and his son Lawrence in 1913-1914 founded the analysis of crystal structure by means of X-rays. If the fundamental discovery of the wave aspect of X-rays, as evidenced by their diffraction in crystals, was due to [von Laue](#) and his collaborators, it is equally true that the use of X-rays as an instrument for the systematic revelation of the way in which crystals are built was entirely due to the Braggs.

How Diffraction Works



Diffraction of X-Rays

Bragg's Law

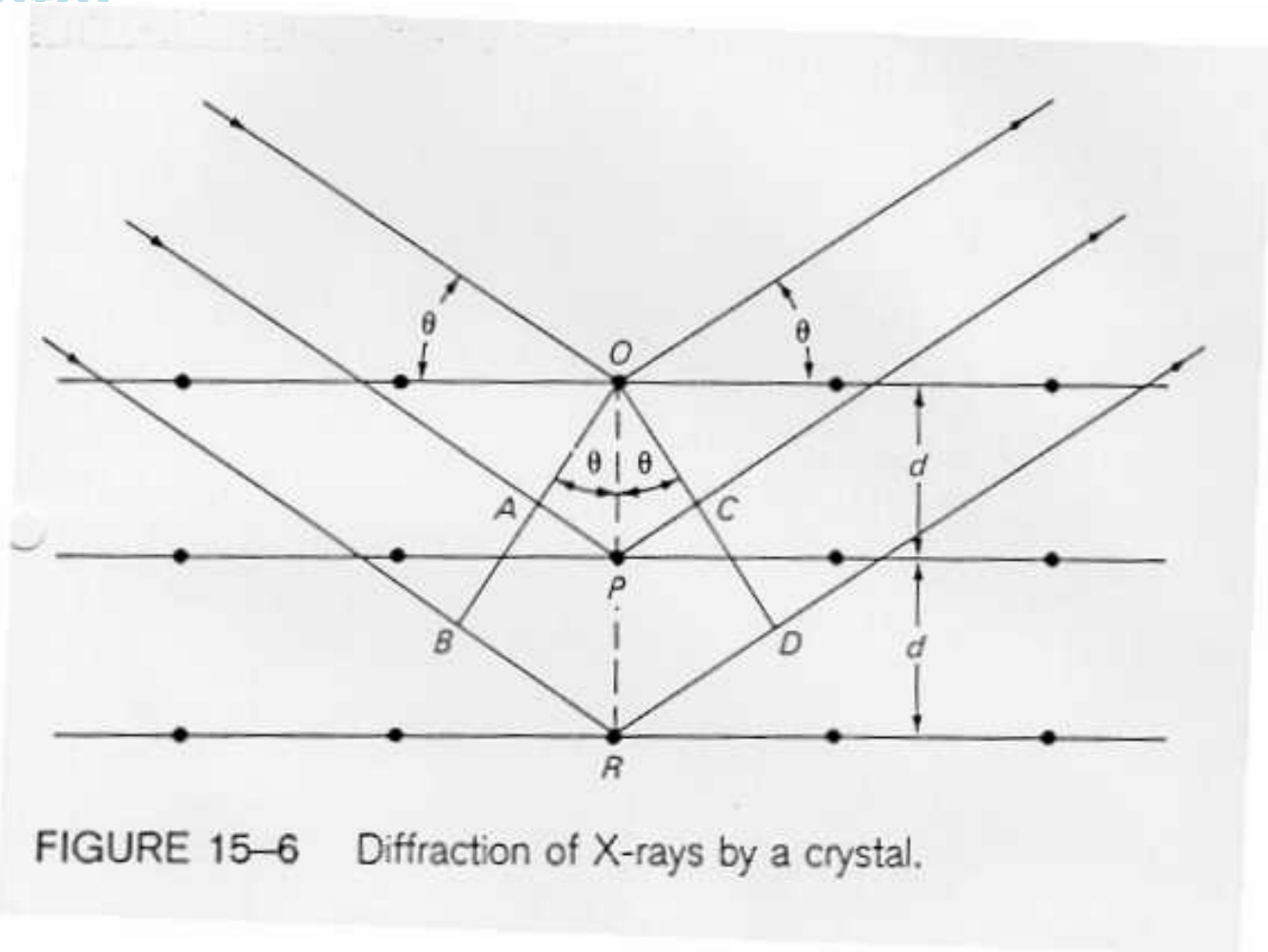
when $AP + PC = n\lambda$ scattered radiation will be "in phase"

$$AP = PC = d \sin \theta$$

$$n \lambda = 2 d \sin \theta$$

Diffraction of X-Rays

Bragg's Law "Diffraction of X-rays by a crystal"



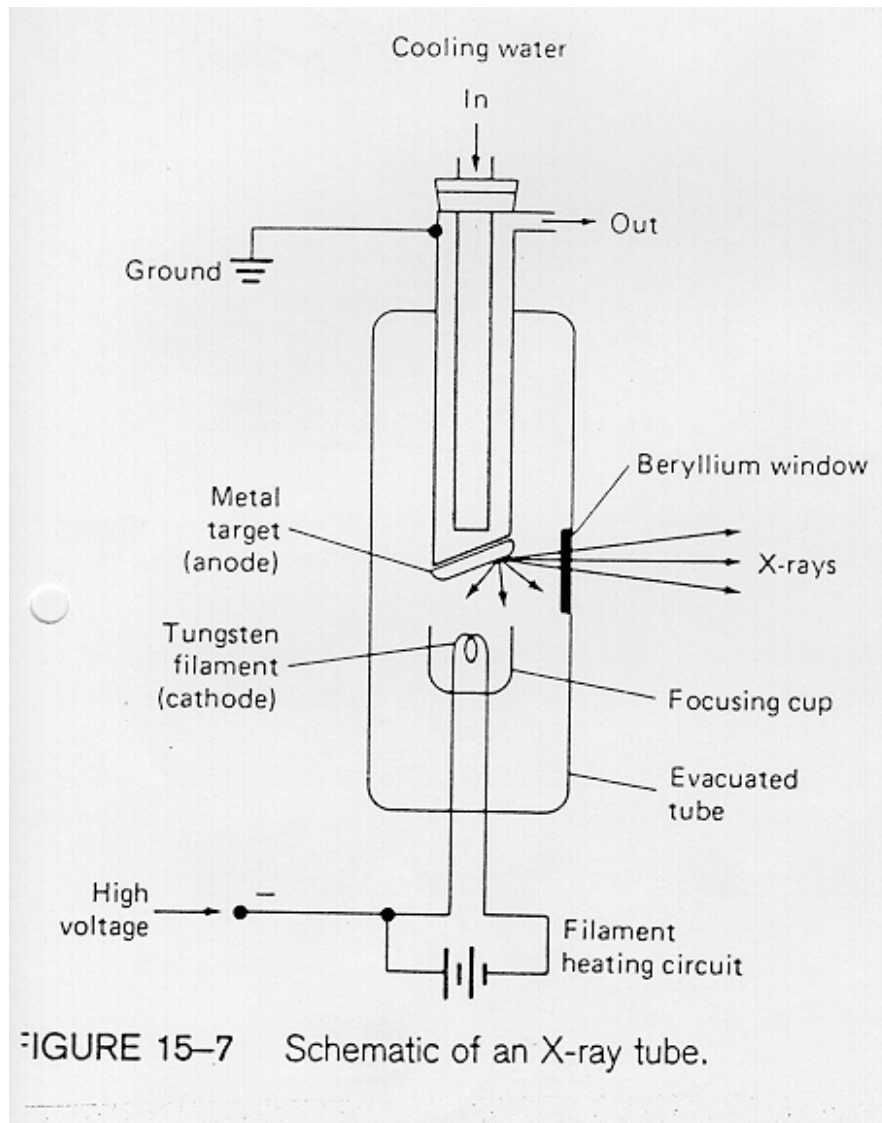
Instrument Components

5 basic components

1. source
2. device for restricting wavelength range
3. sample holder
4. radiation detector
5. signal processor and readout

Sources

"Schematic of
an X-ray
tube."



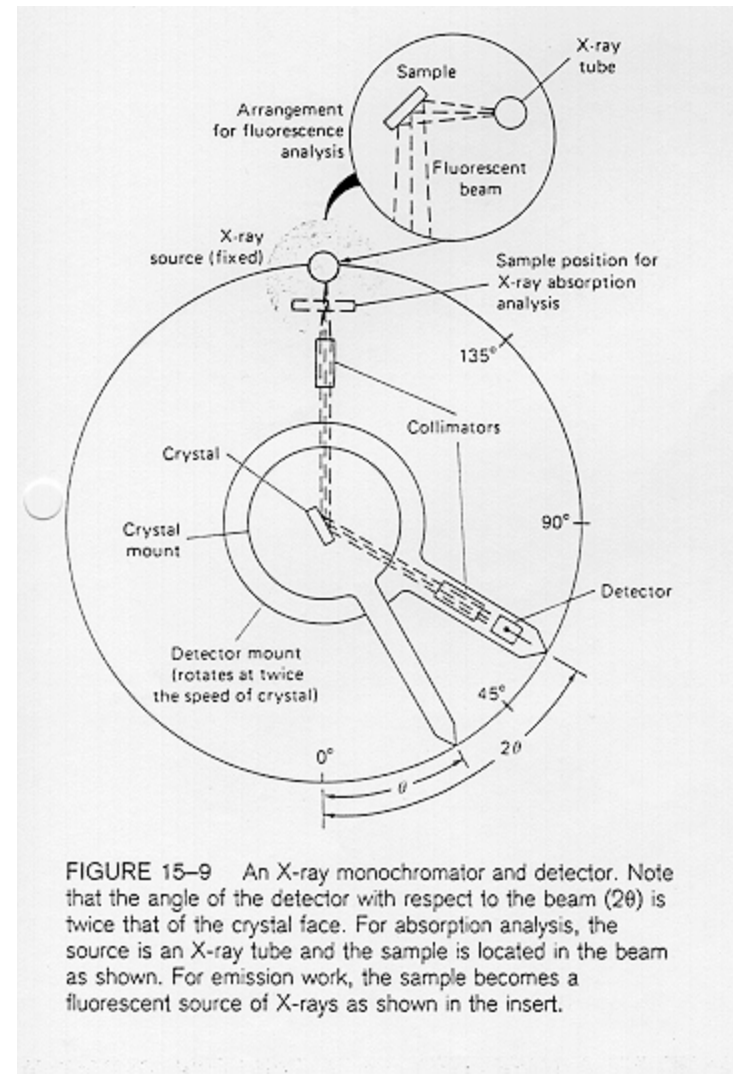
“Monochromator”

Device for restricting wavelength range

- filter => thin metal, element to the left in the Periodic Table
- collimators & slits

X-ray Monochromator

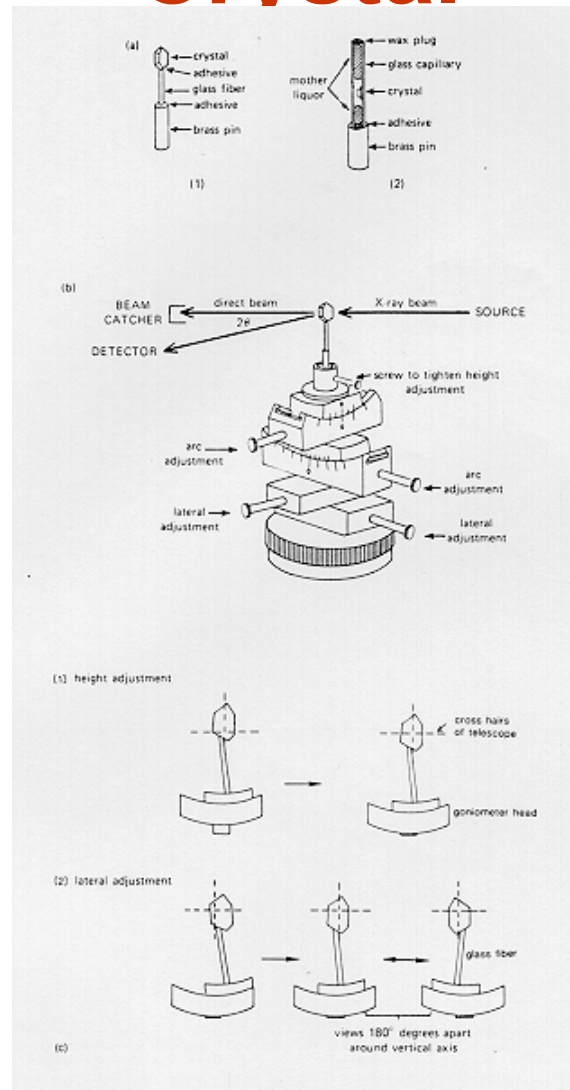
“An X-ray monochromator and detector. Note the angle of the detector with respect to the beam (2θ) is twice that of the crystal face. For absorption analysis, the source is an X-ray tube, and the sample is located in the beam as shown. For emission work, the sample becomes a fluorescent source of X-rays as shown in the inset.”



Sample Holder

- as crystal moves θ , detector moves 2θ
- goniometer head for single crystal
- cup for powder sample

Goniometer Head for Single Crystal



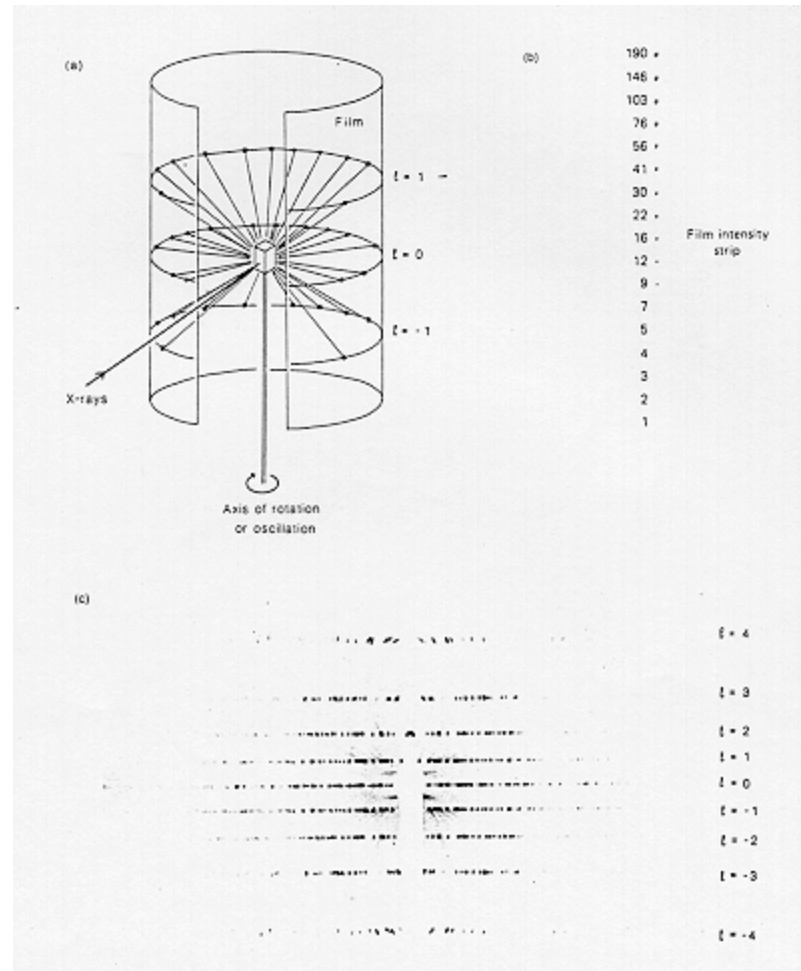
Radiation Detector

X-ray film

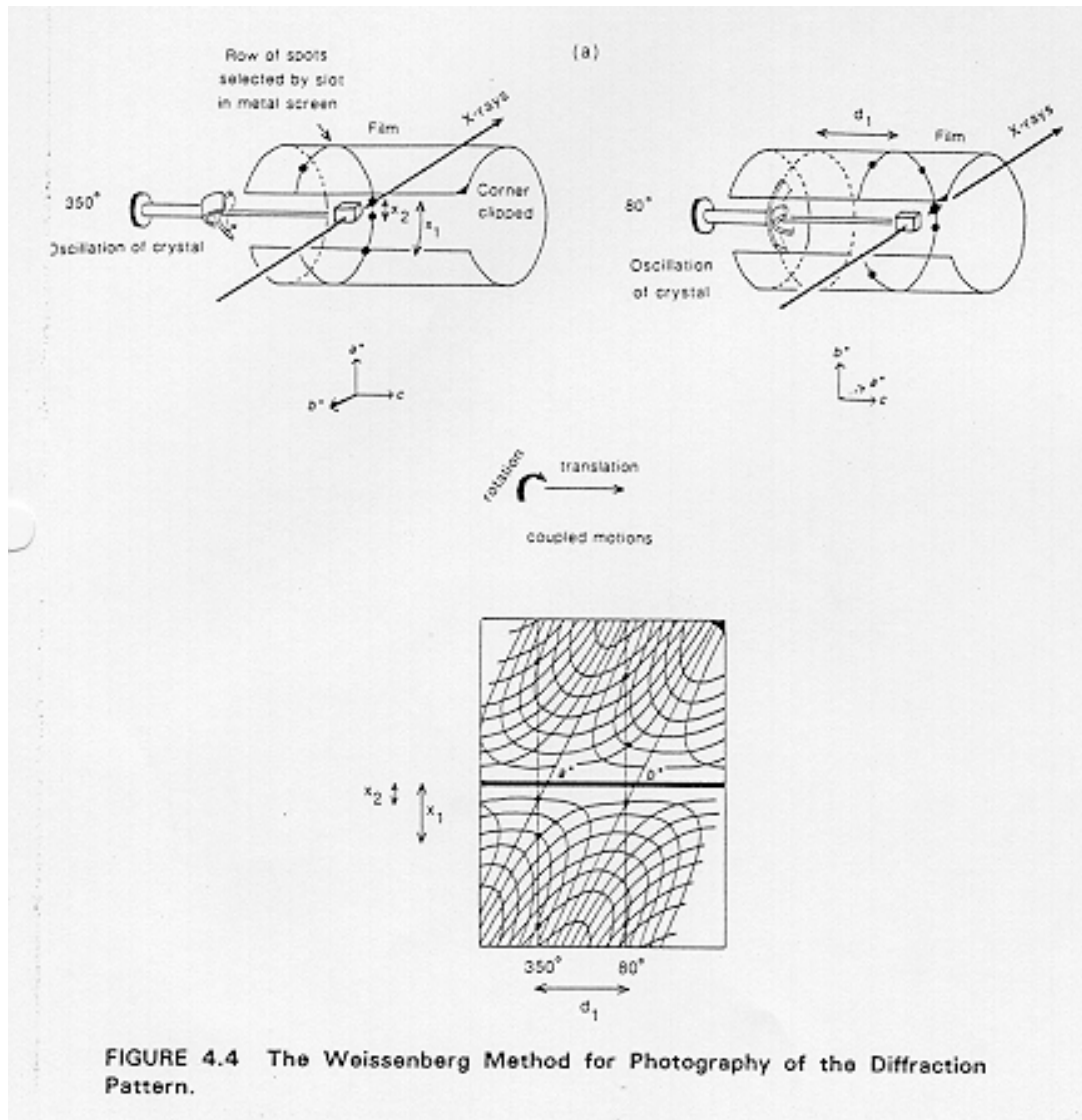
now used mainly for unit cell
dimension and space group
determinations

- Precession camera
- Weissenburg

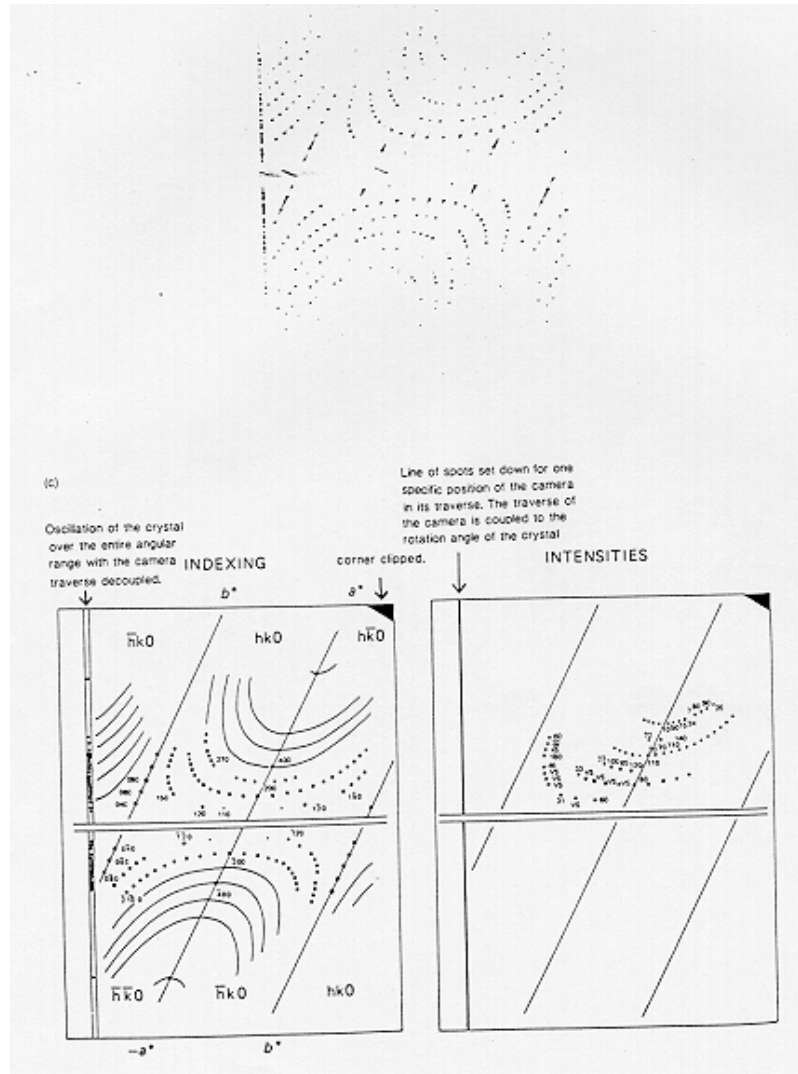
Weissenburg



Weissenburg



Weissenburg



Radiation Detector

Electrical Detectors

1. gas filled detectors

- gas is ionized by X-rays, conducts

2. scintillation counters

- X-rays strike phosphors which give off light
 - originally => counted flasks
 - now => photomultiplier tube used to detect light

Radiation Detector

Electrical Detectors

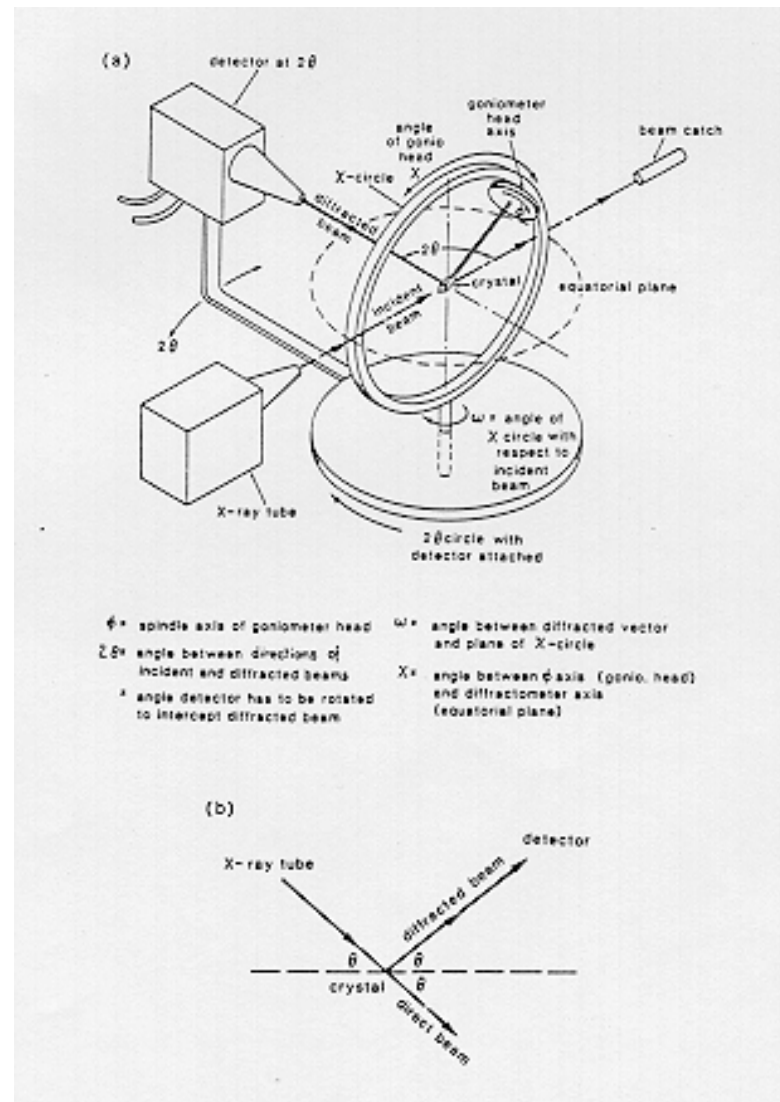
3. semiconductor detectors

- lithium drifted silicon detectors
- charge-coupled device (CCD)

Signal processor & Readout devices

- high speed computer

Automatic Diffractometer



X-ray Diffraction

Information provided by X-ray diffraction:

1. Declare that structures are isostructural.
2. Identify unknowns
3. Determine crystal structure

Isostructural

- Use powder pattern
- measure Bragg angle, θ
- calculate d spacing
- match d spacing with known structure

TABLE VII
LATTICE SPACINGS OF METAL SQUARATES IN Å

$M(III)(OH)(C_4O_4) \cdot 3H_2O$ (2)	$V(III)(OH)(C_4O_4) \cdot 3H_2O$	$V(III)(OH)(C_4O_4) \cdot 2H_2O$	$V(III)(OH)(C_4O_4)$
7.72	7.72	7.57	
6.76	6.61		6.65
6.40	6.37	6.28	
6.16	6.18		
5.75	5.72	5.70	5.51
5.19	5.17	5.17	5.04
4.56	(4.53)		
4.25	4.24	4.23	
3.95	3.96	3.95	3.93
3.70	3.70	3.66	
3.43	3.44	3.41	3.28
3.25	3.23	3.22	
3.13	3.14	3.12	
3.04	3.03	3.03	
2.84	2.84	2.82	
2.74	2.76	2.73	
2.68	2.66	2.66	
2.58	2.58	2.57	2.54
2.48	(2.49) (2.46)	2.48	2.45
2.41	2.39	2.40	
2.29	2.29	2.29	
2.16	2.15	2.15	

Identify Unknowns

- use powder pattern
- measure Bragg angle, θ
- calculate d spacing
- match d spacing with ASTM data

Data Sheet for Powder Data

End of run ^{II} 4162

<u>2θ angle</u>	<u>θ</u>	<u>$\sin \theta$</u>	<u>d</u>	<u>ASTM card # 1-11293</u>
24.3	12.2 (12°12')	0.21132	3.65	3.65
32.95	16.48 (16°29')	0.28374	2.71	2.70
36.2	18.1 (18°6')	0.31068	2.48	2.47
41.25	20.63 (20°38')	0.35239	2.19	2.18
49.85	24.98 (24°59')	0.42235	1.83	1.83
54.0	27.0 (27°0')	0.45399	1.70	1.69
63.3	31.7 (31°42')	0.52547	1.46	1.47
65.25	32.63 (32°38')	0.53926	1.43	1.43
				V ₂ O ₃

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Determine Crystal Structure

- use single crystal data
- calculate d spacing, unit cell dimensions
- index reflections
- propose structure
- match calculated data to experimental data

Single Crystal X-ray Analysis

THE X-RAY DIFFRACTION EXPERIMENT DETERMINING MOLECULAR STRUCTURES

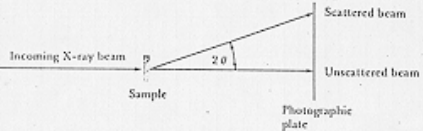
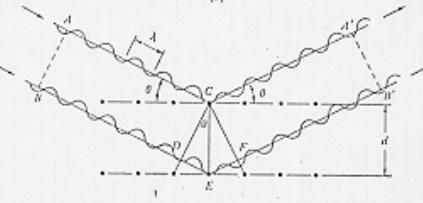
EXPERIMENTAL

① electron density in cell at x, y, z (atom positions) = $\sum_{\text{all hkl}} \downarrow F_{\text{obs}}^{\text{hkl}} \cos 2\pi(hx+ky+lz)$

X-ray lab meas each reflection

Prelim meas → Unit cell dimensions



MODEL

② $F_{\text{calc}}^{\text{hkl}}$ (for model) = $\sum_{\text{all atoms}} (\text{scat power})(\text{temp fac}) \cos 2\pi(hx+ky+lz)$

- Start- Position first atom(s)
 - Vector map analysis (Patterson)

Good for heavy atom structure
 - Direct method (MULTAN)

Gambling on statistics
- Find other atoms (Fourier maps)

Contours of electron density

Use phases of ② in ①
- Refine atom positions and temp.

least squares (300x300!)

h	k	l	F _{obs}
8.	2.	-0.	71.74
12.	4.	-9.	39.04
12.	6.	-9.	18.88
8.	4.	-6.	63.36
4.	2.	-3.	138.34
12.	8.	-9.	20.08
8.	6.	-6.	37.08
8.	8.	-6.	62.90
4.	4.	-3.	54.56
8.	10.	-6.	24.80
4.	8.	-3.	63.72
4.	8.	-3.	79.94
4.	10.	-3.	42.11
17.	1.	-13.	24.99
17.	3.	-13.	26.03
13.	3.	-10.	36.07
13.	5.	-10.	20.23
13.	7.	-10.	24.74
9.	1.	-7.	54.17
9.	3.	-7.	11.58
9.	5.	-7.	26.14
9.	7.	-7.	25.30
9.	9.	-7.	33.55
14.	0.	-11.	11.46
14.	2.	-11.	56.27
14.	4.	-11.	51.38
12.	0.	-9.	71.54
8.	0.	-6.	41.63
4.	0.	-3.	202.81
16.	2.	-12.	8.73
12.	4.	-12.	28.04
16.	4.	-12.	22.55
18.	2.	-6.	47.41
12.	4.	-6.	39.04
12.	6.	-6.	18.88
8.	4.	-6.	63.36
4.	2.	-3.	138.34
12.	8.	-9.	20.08
8.	6.	-6.	37.08
8.	8.	-6.	62.90
4.	4.	-3.	54.56
8.	10.	-6.	24.80
4.	8.	-3.	63.72
4.	8.	-3.	79.94
4.	10.	-3.	42.11

F_{calc}

Usually 2,000-10,000 refl

1. Start- Position first atom(s)

- Vector map analysis (Patterson)

Good for heavy atom structure
- Direct method (MULTAN)

Gambling on statistics

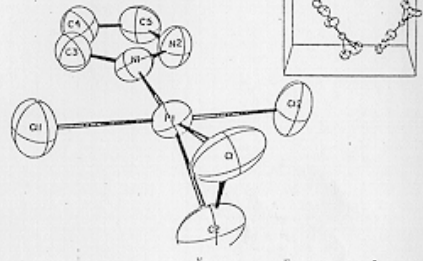
2. Find other atoms (Fourier maps)

Contours of electron density

Use phases of ② in ①

3. Refine atom positions and temp.

least squares (300x300!)



$R = \frac{\sum \Delta F}{\sum F_{\text{obs}}} \approx \text{\% error (hope for 3-5\%)}$

$\frac{\text{Data}}{\text{Unknowns}} = \frac{\text{reflections}}{\text{atom xyz, temp}} = \frac{5-15}{1}$

Table 2. Selected interatomic distances (Å) and angles (°) with e.s.d.'s in parentheses

	Pt	0-11534 (9)	0-05943 (6)	0-22306 (5)
Pt-Cl(1)	0-3658 (7)	0-1614 (5)	0-1733 (5)	
Pt-Cl(2)	2-282 (6)	Cl(1)-Pt-Cl(2)	178.6 (2)	
Pt-Cl(3)	2-279 (6)	Cl(1)-Pt-N(1)	89.4 (4)	
Pt-C(1)	2-13 (2)	Cl(2)-Pt-N(1)	90.9 (4)	

Electron Density Data

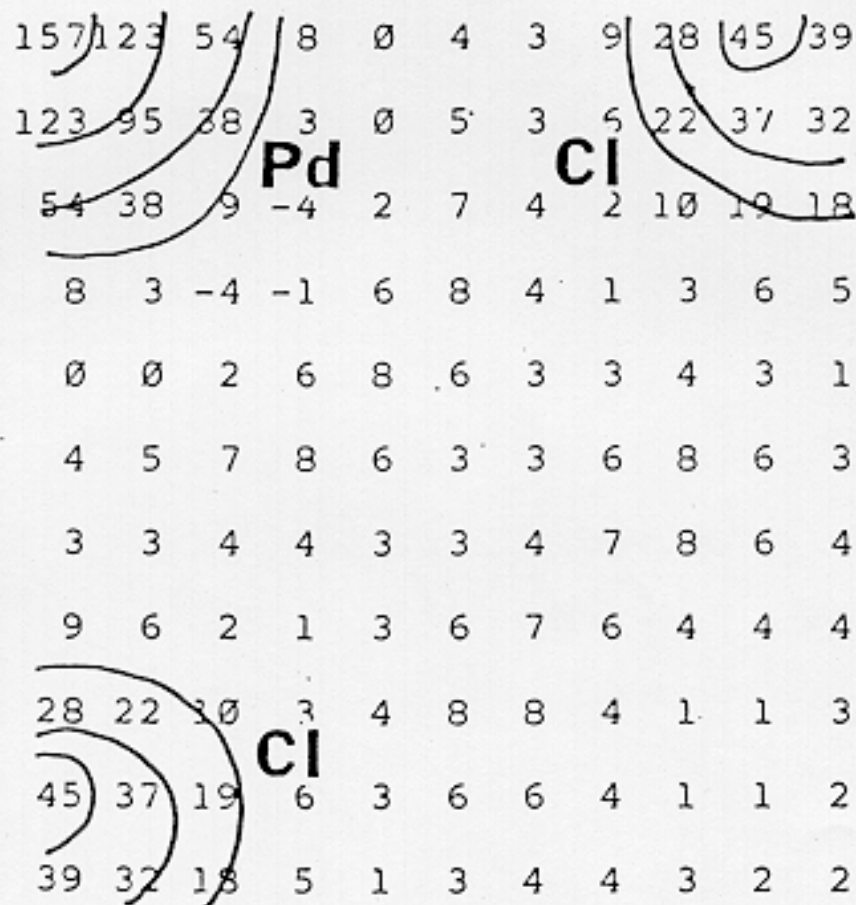
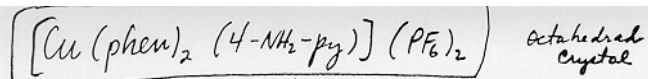


Figure 2. Section of electron density map showing Pd and Cl atoms.

Single Crystal X-ray Analysis



Formula: $\text{Cu}(\text{C}_{12}\text{H}_8\text{N}_2)_2(\text{C}_5\text{H}_6\text{N}_2)(\text{PF}_6)_2$

Space Group: Orthorhombic $Pbca$ (#61)
 $a = 32.571(7)$ $b = 11.00$

$$a = 32.574(7) \quad b = 16.012(3) \quad c = 13.648(3)$$
$$\alpha = \beta = \gamma = 90.0^\circ$$
$$V = 7.118,5 (6) \quad \text{unit cell volume}$$
 $z = 8.0$ number of molecules/unit cell

$\mu = 7.922$ absorption coefficient

$\rho = 1.508$ calculated density

Programs: START

7168 reflections collected

168 standards $\begin{bmatrix} 4 & 0 & \bar{6} \\ 14 & \bar{2} & \bar{2} \\ 4 & \bar{6} & \bar{3} \end{bmatrix}$

2719 unobserved

2719 unobserved [4 6 3]

 $\rightarrow 25^\circ 2\theta$
$$h \quad 0 \rightarrow 38$$
$$k \quad 0 \rightarrow -19$$
$$2 - 16 \rightarrow 0$$

STDPLT

exposure time 53.0 hrs

change in standards - 1.4%

REJECT

Removed 273 from centering collection

ROTATE

$$h \rightarrow l / l \rightarrow h / k \rightarrow -k$$
$$\begin{vmatrix} 0 & 0 & 1 \\ 0 & -1 & 0 \\ 1 & 0 & 0 \end{vmatrix} \begin{vmatrix} h \\ k \\ l \end{vmatrix}_{\text{old}} = \begin{vmatrix} h \\ k \\ l \end{vmatrix}_{\text{new}}$$

old new

Her

size of tetrahedron
 $.48 \times .52 \times .54 \times .54$

25 reflections

$$18^\circ < 2\theta < 20^\circ$$

3330 reflections
used within

36

REJECT

#1 (b glide) OKL; $k=2n$

#5 (c glide) hol; $l = 2n$

#9 (a glide) $hk0$; $h=2n$

592 reflections rejected

6303 reflections kept

PATTERSON

Heavy atom vector search

Trans-Bisbisulfitetetraamineruthenium(II)

